RELATIONSHIP BETWEEN SUBSTITUENT ELECTRONEGATIVITY AND FIELD PARAMETER IN THE ALIPHATIC SERIES. INTRODUCTION OF CHARGE SEPARATION PARAMETER (λ)

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The problem of non-proportionality between the substituent field parameter (σ_F) and substituent electronegativity (Δ_{ι} or σ_{χ}) was clarified by the introduction of the 'charge-separation parameter' (λ), which is the component for the direction of the H—X axis of the distance between positive and negative poles of the dipole in the H—X molecule. Thus σ_F was correlated with Δ_{ι} or σ_{χ} by the equation $\sigma_F = a \Delta_{\iota} \lambda$ (or $\sigma_F = a' \sigma_{\chi} \lambda$). The above proposal was further supported by performing an energy decomposition analysis for the isodesmic reaction in the isolated molecule system (X—H…HNH₃ or X—H…HCO₂) at shorter distances (2·0-4·5 Å). It was further shown that field parameters such as σ_i , F and $\sigma_{F(theor)}$, and the pK_a values in the series of aliphatic acids, and spectral data (UPS and ¹³C-SCS) were also well correlated with Δ_{ι} or $\sigma_{\chi} \lambda$. It is concluded that λ and Δ_{ι} or σ_{χ} are essential parameters for interpreting the electrostatic field effect in aliphatic substituent effects, and that the transmission due to the σ -inductive effect is considered to be not as significant as the field effect after a few bonds away from the substituent.

INTRODUCTION

The concept of the inductive effect was first introduced as the through- σ -bond effect (i.e. the σ -inductive effect) by Robinson^{1a} and Ingold.^{1b} Currently, however, the polar substituent effect in aliphatic systems is described as the sum of through- σ -bond and field effects, and that in aromatic systems as the sum of field, resonance^{2,3} and π polarization effects.^{4,5}

The σ -inductive effect originates from bond polarization due to the difference in electronegativities between the substituent and the adjacent atom, and is transmitted through progressive but diminishing σ -bond polarization.^{6,7} On the other hand, the field mechanism for transmission of substituent effects is mainly attributed to the Coulombic field interaction between the dipole of the substituent and the charge of the probe centre (dipole-charge interaction).⁸ The transmission due to the σ -inductive effect has been considered to be less significant than the field effect after two bonds away from the substituent.⁹

Recently, non-linearity in the plot of the field parameters (σ_F or σ_1) of the dipole moments (p_{MeX}) of CH₃X against the group electronegativities (χ_X) or the inductive substituent parameters (ι) has been reported by several workers.^{3b,10,11} Further, it has not been explained why the field effect is dominant for the ΔpK_a values¹² of XCH₂CO₂H, while the electronegativity of a substituent correlates linearly with the proton chemical shift parameter ($\delta_{CH_2} - \delta_{CH_3}$) in an apparently similar system, XCH₂CH₃.¹³

These facts led us to examine the reason for the nonproportionality between the field parameter and electronegativity. Then we attempted to obtain information regarding the interaction between the point charge of the probe centre and the pure dipole 'substituent'^{14,15} using the isodesmic reaction (1), and applied energy decomposition analysis¹⁶ to the isodesmic reaction (1) for the molecular pair 1, composed of the pure dipole 'substituent,' H–H, and point charge as the probe centre, where the field effect would be dominant.

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In 1, *ne* represents the charge on the pure dipole 'substituent,' Λ the distance between positive and negative charges in the pure dipole 'substituent' and θ the angle between the dipole and the z-axis. From the result thus obtained, a linear relationship between the electrostatic field energy (*ES*) and the z-component of the dipole moment ($p_z = ne\Lambda \cos \theta$; see 1) was observed, but there was no similar relationship between *ES* and the charge (*ne*) on the dipole 'substituent.' Consequently, the major reason for the non-proportionality^{10,11} between the field parameters (σ_F , σ_I and p_{MeX}) and the electronegativity or inductive substituent parameter (σ_X , $\Delta_i = \iota_X - \iota_H$) may be clarified by means of this analysis.

A theoretical scale of the field parameter $[\sigma_{F(\text{theor})}]^{17}$ has recently been derived from MO calculation (at the 4-31G level) for the proton transfer reaction (2) in the molecular pair (2), where r' = 4.5 Å and above;¹⁸ r' is the distance between the hydrogen atom of the H-X molecule and the nitrogen or carbon atom of NH₄⁺ (2) or HCO₂⁻ (3). However, the studies concerned were made under the assumption that the electrostatic interaction is dominant at such longer distances.

Strictly, in the interaction between the substituent and probe centre, different types of interactions contribute to the total interaction energy (ΔE) , ¹⁶ i.e.

$$\Delta E = ES + PL + CT + EX + MIX$$

where ES is electrostatic energy, PL polarization energy, CT charge-transfer energy, EX electronexchange repulsion energy and MIX the higher order terms. The components of such interactions are often complicated at shorter distances. Therefore, we also performed energy decomposition analysis¹⁶ for the proton transfer isodesmic reactions (2) and (3) in molecular pairs 2 and 3 at several distances.

$$(X-H\cdots NH_3) + (H-H\cdots H\dot{N}H_3) \longrightarrow (H-H\cdots H\dot{N}H_3) + (X-H\cdots H\dot{N}H_3)$$
(2)

The result of the analyses shows that the electrostatic energy terms (ES) in reactions (2) and (3) are correlated, even at a short distance (r' = 2.5 Å), with the dipole parameter $\Delta \iota \lambda$,¹⁹ where λ is the z-component of the distance (Λ) between the positive and negative poles in the H-X molecule (i.e. $\lambda = \Lambda \cos \theta$; cf. 1), namely the charge separation parameter.

In order to ascertain whether the charge separation parameter $(\lambda)^{19}$ is independent of the systems or not, we also examined the utility of the parameter, $\Delta i \lambda$ or $\sigma_{\chi} \lambda$,¹⁹ for the observed data such as relative pK_a values (ΔpK_a) in substituted aliphatic acids,^{20,21} UPS data²² and carbon-13 substituent chemical shifts (¹³C-SCS) in aliphatic derivatives.²³

CALCULATIONS AND RESULTS

MO calculations were performed by the *ab initio* method at 4-31G and 6-31G basis levels using the GAUSSIAN-80^{24a} and IMSPAC^{24b} program series. Molecular geometries were taken from observed values.²⁵ All calculations were carried out with a FACOM M-382 computer at the Nagoya University Computation Center.

The pure dipole 'substituent' having only positive and negative point charges was taken to be the same as that used in previous papers.^{14,15} The probe centre and the centre of the pure dipole 'substituent' were located on the H-H molecular axis as shown in 1. In the hypothetical system 1, the total energy of interaction is composed of electrostatic (*ES*) and polarization (*PL*) energies. We chose $5 \cdot 0$ Å as the distance between the probe centre and the centre of the H-H bond (see 1). The centre of the dipole was always fixed at $1 \cdot 36$ Å away from the hydrogen atom H(1) on the z-axis, as used by Vorpazel *et al.*¹⁵ When $\Lambda = 0.72$ Å and $ne = 1 \cdot 0$, the dipole moment of the pure dipole 'substituent' nearly corresponds to that of nitromethane. We used $\Lambda = 0.72$, $1 \cdot 0$ and $1 \cdot 5$ Å, $ne = 1 \cdot 0$, $0 \cdot 5$ and $0 \cdot 3$ units and $\theta = 0^{\circ}$, 30° , 60° and 90° (see 1).

Table 1 summarizes the results calculated at the 4-31G level for reaction (1) in the case of the negative point charge in 1. The energies for the isodesmic reaction (1) (i.e. E_A , E_B , E_C and E_D), the electrostatic interaction energies (ES_D and ES_B) and the relative energy components ($\delta\Delta E$, δES and δPL) for the energy decomposi-

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Table 1. Energy decomposition analysis for the isodesmic reaction (at the 4-31G level)

$$H-H(+-,\theta) + (-)\cdots H-H \rightarrow H-H + (-)\cdots H-H(+-,\theta)$$
(A) (B) (C) (D)

No.	neª	Λª/Å					Relative	e energy com kcal mol ^{-1e}	ponent/	
			$\theta^{a}/^{\circ}$	$E_{\rm A}{}^{\rm b}/{\rm a.u.}$	$E_{\rm D}^{\rm c}/{\rm a.u.}$	$ES_{D}^{d}/a.u.$	δΔΕ	δES	δPL	$= ne \lambda \cos \theta$ $= ne \lambda / debye (D)$
1	_ I	f	f	- 1 · 12676 ^g	- 1 · 12754 ^h	- 1 · 12713 ⁱ	$0.00 (-0.49)^{j}$	$0.00 (-0.23)^{k}$	$0.00 (-0.26)^{1}$	0.00
2	1.0	0.72	0	- 1 • 84658	- 1 • 86041	-1.86004	~ 8 ⋅ 19	-8.21	0.02	3.46
3	1.0	0.72	30	- 1 • 84939	- 1 • 86131	- 1 • 86093	- 7.02	- 7.04	0.02	3.00
4	1.0	0.72	60	-1.85452	- 1 • 86164	-1.86124	- 3.98	- 3 · 99	0.01	1.73
5	1.0	0.72	90	- 1 • 86171	- 1 · 86250	- 1 • 86209	- 0.01	-0.01	0.00	0.00
6	1.0	1.00	60	-1.64814	- 1 • 65749	-1.65711	- 5 • 35	- 5 • 37	0.02	2.40
7	1.0	1 - 50	60	-1.47292	- 1 · 48559	-1.48520	- 7 • 46	-7.48	0.02	3.60
8	0.5	0.60	60	-1.34338	-1.34684	- 1 • 34643	- 1.68	-1.68	0.00	0.72
9	0.5	1.00	30	- 1 • 24595	- 1 • 25444	-1.25405	- 4 · 84	- 4.85	0.01	2.08
10	0.3	0.60	60	- 1 · 20368	-1.20607	-1.20566	- 1.01	-1.01	0.00	0.43
11	0.3	1.00	30	-1.16533	- 1 · 17074	$-1 \cdot 17035$	- 2.90	- 2.92	0.02	1 - 25

^aCf. 1.

^b Total energy for system A.

^c Total energy for system D perturbed with negative point charge.

^d Electrostatic energy for system D perturbed with negative point charge.

 ${}^{e}\delta\Delta E = (E_{\rm D} - E_{\rm A}) - (E_{\rm B} - E_{\rm C}) = \Delta E_{\rm subs1} - \Delta E_{\rm H}; \quad \delta ES = ES_{\rm subs1} - ES_{\rm H}, \quad ES_{\rm subs1} = ES_{\rm D} - E_{\rm A}, \quad ES_{\rm H} = ES_{\rm B} - E_{\rm C}; \quad \delta PL = \delta\Delta E - \delta ES.$

^fUnsubstituted system.

 ${}^{g}E_{C}$.

 ${}^{h}E_{B}$.

ⁱES_B.

 $^{j}\Delta E_{\rm H} = E_{\rm B} - E_{\rm C}$.

 $ES_{\rm H} = ES_{\rm B} - E_{\rm C}$

 $PL_{\rm H} = \Delta E_{\rm H} - ES_{\rm H}$

tion analysis are also shown in Table 1. The last column in Table 1 lists values of $ne \Lambda \cos \theta$ (= p_z). A linear relationship between the relative interaction energies ($-\delta\Delta E$) and p_z (= $ne \Lambda \cos \theta$) for 1 is shown in Figure 1. On the other hand, no linear relationship between $-\delta\Delta E$ and *ne* is observed.

Table 2 gives the charge density $(1 - q_H)$ on the hydrogen atom, p_z (= $p \cos \theta$) calculated for the H-X



Figure 1. Linear relationship between the relative isodesmic reaction energies ($\delta\Delta E$) in reaction (1) and $ne \Lambda \cos \theta$ (= p_z) in 1

Table 2. The charge on hydrogen $(1 - q_H)$, z-component of dipole moment (p_z) and charge separation parameter (λ) in H-X molecule

	4	4-31G		6-31G				
x	(1 – q _н)	p _z /D	λ/Å	$(1 - q_{\rm H})$	p_z/D	λ/Å		
CH ₃	0.1522	0.00	0.000	0.1549	0.00	0.000		
NH ₂	0.3042	0.73	0.500	0.3096	0.73	0.495		
OCH ₃	0.3967	1.24	0.651	0.3977	1.24	0.649		
он	0.3936	1.60	0.846	0.4257	1.62	0.796		
СНО	0.1541	1 · 57	2.121	0.1484	1.58	2.221		
F	0.4786	2.28	0.992	0.4820	2.30	0.992		
CF ₃	0.2104	2.17	2.147	0.1972	2.20	2.320		
COCH ₃	0.1559	1.20	1.603	0.1498	1.21	1.682		
CO ₂ H	0.2158	1.34	1.289	0.2093	1.36	1.351		
CO ₂ CH ₃	0.2125	1.72	1.684	0.2076	1.75	1.750		
CN	0.3308	3.25	2.046	0.3336	3.27	2.039		
NO_2	0.4320	3.51	1 · 692	0.4247	3.53	1.733		



Figure 2. Relationship between field parameter, $\sigma_t(g)$, and $\Delta_t \lambda$ or $\sigma_{\chi} \lambda$

molecule and the charge separation parameter (λ) , which was obtained from the equation $\lambda = p \cos \theta / [e(1 - q_H)]$, where p represents the dipole moment of the H-X molecule in place of the group dipole moment of X.

Figure 2 shows the relationship between the field parameter $[\sigma_1(g) = \sigma_F]^{26}$ and dipole parameter $(\Delta \iota \lambda \text{ or } \sigma_\chi \lambda)$.

Tables 3 and 4 give the interaction energies (ΔE) and

Table 3. Energy decomposition analysis for $2 (X=NO_2)$ (at the 4-31G level)

	Energy/kcal mol ⁻¹								
r'/Å	ΔE	ES	PL	CT	EX	MIX			
4.5	9.78	10.24	-0.43	- 0.03	0.00	0.00			
4.5	$(0.87)^{a}$	(0.95)	(-0.05)	(-0.03)	(0.00)	(0.00)			
3.5	14.62	16.19	-1.15	-0.58	0.05	0.11			
2.5	27.10	30.55	- 5 • 47	- 3.62	3.51	2.13			
2.5	(6·07) ^a	(5.65)	(-2.14)	(-2.84)	(4.79)	(0.61)			
2.25	36.10	37.70	- 9·87	- 6.49	9.43	5.33			
2.0	54.72	49.02	~ 20.06	-20.06	24.67	21.15			

^a The results for the neutral molecule system $(X - H - NO_2)$ are given in parentheses.

Table 4. Energy decomposition analysis for 3 (X=F) (at the 4-31G level)

	Energy/kcal mol ⁻¹								
r'/Å	ΔE	ES	PL	СТ	EX	MIX			
4.5	- 4.79	- 4 • 54	-0.13	-0.13	0.00	0.01			
4.5	$(1 \cdot 10)^{a}$	$(1 \cdot 16)$	(-0.04)	(-0.02)	(0.00)	(0.00)			
3.5	-7.53	-6.53	-0.46	- 0.82	0.25	0.03			
2.5	-7.52	- 11.02	$-4 \cdot 21$	- 4 · 13	10.05	1.79			
2.5	$(8.79)^{a}$	(7.78)	(-2.29)	$(-3 \cdot 12)$	(5.48)	(0.94)			
2.25	-1.36	- 12.97	-8.80	- 8.60	23.38	5.63			
2.0	17.09	-13.18	- 19 · 23	$-22 \cdot 20$	53.05	18.65			

^a The results for the neutral molecule system $(X - H \cdots HCO_2H)$ are given in parentheses.

the component terms (i.e. ES, PL, CT, EX and MIX) calculated at several distances $(2 \cdot 0 - 4 \cdot 5 \text{ Å})$ for 2 $(X = NO_2)$ and 3 (X = F) using the 4-31G basis set. The corresponding results of the energy decomposition analyses for the neutral molecule system (i.e. $X-H\cdots H-NH_2$ and $X-H\cdots H-CO_2H$) at $r' = 2 \cdot 5$ and $4 \cdot 5$ Å are shown in parentheses.

Figure 3 shows the distance dependence of the interaction energy (ΔE) and the component energies for 3 (X = F). The interaction energies (ΔE) and their component terms for the isodesmic proton transfer reactions [(2) and (3)], together with the corresponding relative interaction energies [$\delta \Delta E = (\Delta E_X - \Delta E_H)$] and their relative component terms [$\delta ES = (ES_X - ES_H)$, $\delta PL = (PL_X - PL_H)$, $\delta CT = (CT_X - CT_H)$, etc.] at r' = 4.5 Å, and the corresponding values at r' = 2.5 Å are given in Tables 5 and 6, respectively.



Figure 3. Distance dependence of each of the energy components of the intermolecular interaction energy in the $F-H\cdots HCO_2^-$ system

r'/Å		Energy (kcal mol ⁻¹)							
	х	δΔΕ	δES	δΡL	δCT	δΕΧ	δΜΙΧ		
4.5	н	0.00	0.00	0.00	0.00	0.00	0.00		
		$(-0.09)^{a}$	(0.24)	(-0.32)	(-0.01)	(-0.01)	(0.01)		
	F	6.09	5.92	0.16	0.02	0.01	-0.02		
	NO ₂	9.00	9.05	-0.06	0.01	0.01	-0.01		
	NH ₂	1.60	1.62	-0.05	0.01	0.00	- 0.01		
	CN	6.28	6.42	-0.16	0.02	0.00	0.00		
2.5	н	0.00	0.00	0.00	0.00	0.00	0.00		
		$(-2 \cdot 16)^{a}$	(2.23)	(-3.91)	(-0.87)	(-1.33)	(1.72)		
	F	17.55	15.96	2.46	- 0.27	0.18	-0.78		
	NO ₂	23.19	22.67	0.58	0.09	0.02	-0.20		
	NH ₂	3.96	4.33	-0.05	-0.73	-0.03	0.41		
	CN	15.12	15.29	0.18	0.18	-0.19	-0.34		

Table 5. Energy decomposition analysis for the isodesmic reaction (2) (at the 4-31G level)

^a Values in parentheses are energy values of each term when X = H.

r′/Å 4·5											
	X	δΔΕ	δES	δPL	δCT	δΕΧ	δΜΙΧ				
	н	$0.00 (-0.41)^{a}$	0.00 (-0.22)	0.00 (-0.14)	0.00	0.00 (0.01)	0.00				
	F NO₂	- 5·48 - 8·49	-5.48 -8.26	0.05 -0.12	- 0.05 - 0.17	-0.01 -0.06	0·01 0·12				
	NH2 CN	-1.85 -6.15	-1.80 -5.93	0.00 -0.10	-0.04 - 0.10	0.00 0.00	-0.01 - 0.02				
2.5	Н	$0.00 (-0.17)^{a}$	0·00 (-4·22)	0·00 (0·17)	0.00 (-2.58)	0·00 (5·79)	0·00 (0·67)				
	F NO₂	$-16 \cdot 14$ -22 \cdot 69	-14.58 -20.51	$-2 \cdot 09$ 3 \cdot 30	1·57 0·70	$-1 \cdot 22 - 0 \cdot 44$	0·18 0·86				
	NH₂ CN	-5.02 -14.73	-4·69 -14·01	-0.75 -2.24	1 · 30 0 · 74	-0.32 0.26	-0.56 0.52				

Table 6. Energy decomposition analysis for the isodesmic reaction (3) (at the 4-31G level)

^a Values in parentheses are energy values of each term when X = H.

Table 7 summarizes the results of statistical analyses for the relative pk_a values (ΔpK_a) of various series of substituted aliphatic carboxylic acids and ammonium salts,^{20,21} ionization potentials (*IP*) or relative rate of methylation of 4-substituted quinuclidines,^{22,31} ¹³C-SCS in the phenyl *p*-carbon of 4-substituted 1-phenylbicyclo[2.2.2]octanes²³ and others²⁹ and relative rate of esterification of substituted acetic acids³⁰ using the dipole parameter ($\Delta i\lambda$ or $\sigma_{\chi}\lambda$).

DISCUSSION

The field parameter (σ_F or σ_1) depends essentially on the group dipole moment of the substituent (p_X) which is correlated with $\Delta \iota \lambda$, whereas the σ -inductive effect is related directly to the group electronegativity (χ_X , σ_X or

 $\Delta \iota$). Therefore, there is no relationship between $\sigma_{\rm F}$ (or $\sigma_{\rm I}$) and σ_{χ} (or $\Delta \iota$).^{10,11}

A decisive answer concerning this non-proportionality was obtained from the following consideration using the results in Table 1. According to the energy decomposition analysis for the case of a negative probe charge, the field energies (ΔE) in the system 1 are almost entirely composed of the electrostatic energy (*ES*) as shown in Table 1, and the contribution of the polarization energy (*PL*) can be ignored. It was previously pointed out¹⁴ that the logarithm of the interaction energy (log ΔE) between molecules X—H and point charge [i.e. (\pm)····H—X) is well correlated with $-\log r$ having a slope of nearly 2 at various distances (r) between the hydrogen atom of X–H and point charge as expected from equation (4). Hence the interaction

		Slo	ope						
Parameter	System	α	β	r	.a	ſ	ſ ^b		Ref.
$\Delta p K_a$	XGCO ₂ H:								
	$G = CH_2$	2.09	4.15	0.963	0.975	0.17	0.14	10	20.21
	$(CH_2)_2$	0.74	1 · 46	0.960	0.970	0.18	0.16	10	27
	(CH ₂) ₃	0.33	0.67	0.983	0-962	0.16	0-22	7	27
	(CH ₂) ₄	0.32	0.69	0.922	0.961	0.32	0.23	6	27
	$CH_2C_6H_4-p$	0.39	0.76	0.947	0-935	0.23	0.28	5	20 ^d
	5	1 • 57	3.02	0.984	0.960	0.15	0.23	6	28
	6	0.35	0.64	0.987	0.996	0.16	0.08	6	20 ^d
	7	0.52	1.03	0.978	0.983	0.15	0.17	5	20
	8	0.72	1.30	0.990	0.991	0.09	0.09	6	20
	9	0.75	1 · 49	0.960	0-976	0.19	0.15	8	20
	10	0.79	1.65	0.980	0.980	0.15	0.15	7	20 ^d
	11	0.58	1.13	0.973	0.990	0.22	0.15	5	20
	$X - G - \dot{N}H_3$:								
	$G = CH_2$	4.35	8.52	0.997	0.997	0.073	0.076	5	20 ^d
	12	2.41	4.68	0.984	0.984	0.12	0.13	11	20 ^d
	13	1.09	2.14	0.927	0.927	0.42	0.42	5	20
IP	14	0.57	1.08	0.995	0.997	0.09	0.07	6	22
¹³ C-SCS	4 (C-4)	0.63	1.27	0.974	0.976	0.15	0.15	9	23
	15(C-4')	-0.97	-1.90	0.991	0.990	0.12	0.13	5	29
$Log(k/k_0)$	$XCH_2CO_2H + Ph_2CN_2$	1.17	2.31	0.989	0.991	0.17	0.16	6	20, 30°
-0. (0)	$XCH_2CO_2H + Ph_2CN_2$	1.81	3.56	0.994	0.995	0.12	0.11	6	20, 30 ¹
	14 + Mel	-0.54	-1.05	0.969	0.981	0.19	0.15	10	20, 31 ^d .g

Table 7. Statistical results for $\Delta p K_a$, ionization potential (*IP*), ¹³C-SCS and relative rate $[\log(k/k_0)]$ vs $\Delta i\lambda$ (first value listed) or $\sigma_{\chi\lambda}$ (second value listed)

"Correlation coefficient.

^bGoodness of fit (=SD/RMS, where SD = standard deviation and RMS = root mean square of the data).

'Number of data points.

^d The λ value for the CONH₂ group was estimated from equation (10) as 1.968 Å.

"In EtOH at 25 °C.

¹In Me₂SO at 30°C.

^µ In MeOH at 10 °C.

energies (ΔE) in 1 can be approximately calculated by

$$\Delta E = -(ep \cos \theta)/r^2 \tag{4}$$

$$\Delta E = -e (ne \Lambda) \cos \theta / r^2$$
 (5)

where *e* represents the probe point charge. Accordingly, if the distance (*r*) between the probe charge and the centre of the pure dipole 'substituent' is kept constant (for example, r = 6.73 Å in 1), a linear relationship between ΔE and $p_z(=ne \Lambda \cos \theta)$ will be expected from equation (5). In fact, the relative interaction energies ($\delta \Delta E$) and p_z (= $ne \Lambda \cos \theta = ne \lambda$, cited in Table 1) can be well connected by equation (6) with an excellent correlation coefficient. Since $\delta \Delta E$ is nearly same as δES as shown in Table 1, equation (7) is also given with a comparable precision to that of equation (6) (see also Fig. 1);

$$\delta \Delta E = -2.23 \ ne \ \Lambda \ \cos \theta - 0.067 \tag{6}$$

(r_c = 0.996, f = 0.058, n = 11)

$$\delta ES = -2 \cdot 24 \ ne \ \Lambda \ \cos \theta - 0 \cdot 067 \tag{7}$$

$$(r_{\rm c} = 0.996, f = 0.058, n = 11)$$

In contrast, there is no linear relationship between $\delta\Delta E$ and the charges (*ne*) on the pure dipole 'substituent' as shown in Table 1. Hence it is necessary to explain why σ_F (or σ_I) is not linearly correlated with the substituent electronegativity, σ_{χ} (or $\Delta\iota$), because a linear relationship between fractional charge and electronegativity has been indicated ³² and further the σ_{χ} values have been evaluated from the charge densities on the hydrogen atom $(1 - q_H)$ in compounds X-H, ^{10b} and the inductive substituent parameter $(\iota)^{11}$ are related to $(1 - q_H)$.

Charge separation parameter (λ)

The λ parameter of each substituent listed in Table 2 was obtained from the z-component of the dipole moment, p_z (= $p \cos \theta$), for the molecule H-X and the charge density, $(1 - q_H)$, on the hydrogen atom in the

molecule H-X by an *ab initio* molecular orbital calculation at the 4-31G or 6-31G level.

The p_z values listed in Table 2 are expected to show a linear relationship with field parameters, $\sigma_{I}(g)$, which were derived recently from the acidities of the substituted phenols in the gas phase.²⁶ The results are $\sigma_{I}(g) = 0.191 p_{z}$ ($r_{c} = 0.991$, f = 0.088, n = 10 at the 4-31G level) and $\sigma_I(g) = 0.189 p_z$ ($r_c = 0.991$, f = 0.087, n = 10 at the 6-31G level), indicating almost the same correlation coefficient (r_c) , goodness of fit (f) and slope. The types of substituent groups used in the statistical analysis are H, CH₃, NH₂, OCH₃, CHO, F, CF₃, COCH₃, CN and NO₂. Owing to the lack of evaluation of $\sigma_1(g)$ for the CH₃ group, the σ_1 value given by Charton²⁰ was used, but the substituent CO₂CH₃ is eliminated from this statistical analysis, because the inclusion of this group leads to a significant deviation from the regression lines ($r_c = 0.969$, n = 11 at the 4-31G and 6-31G levels). The reason for this deviation can probably be attributed to an imperfection in the separation of the $\sigma_I(g)$ value into the σ_I and σ_R components, because the correlations with σ_i^{34} and the other data in solution are excellent or fairly good even when the CO₂CH₃ group is included, as mentioned later.

On the other hand, we reported previously³³ a good correlation between the relative inductive substituent parameter ($\Delta\iota$) and (1 – $q_{\rm H}$) in H–X molecules.^{10b} According to equation (6), it is expected that the product of the λ value and $\Delta\iota^{11,33}$ or σ_{χ}^{10b} probably bears a linear relationship to the field parameter ($\sigma_{\rm I}$ or $\sigma_{\rm F}$),²⁶ because the $\sigma_{\rm F(theor)}$ (or $\sigma_{\rm F}$) values have recently been evaluated using an interaction energy of isolated molecule systems.¹⁷ In fact, it was found that the p_z values were correlated with $\Delta\iota\lambda$ ($r_c = 0.968$, n = 13 at the 4-31G level; $r_c = 0.986$, n = 13 at the 6-31G level; $r_c = 0.992$, n = 13 at the 6-31G level).

Figure 2 shows plots of $\sigma_I(g)$ values against $\Delta \iota \lambda$ or $\sigma_{\chi} \lambda$, and the following relationships were obtained with a good correlation coefficient for the 10 substituents mentioned above:

 $\sigma_{I}(g) = 0.479\Delta_{t}\lambda_{4.31G} - 0.023 \qquad (r_{c} = 0.987, f = 0.11)$ (8a)

 $\sigma_{\rm I}({\rm g}) = 0.465 \Delta \iota \lambda_{6-31\rm G} - 0.021 \qquad (r_{\rm c} = 0.982, f = 0.13)$ (8b)

 $\sigma_{\rm I}({\rm g}) = 0.975 \sigma_{\chi} \lambda_{4-31\rm G} - 0.004$ (*r*_c = 0.987, *f* = 0.11) (9a)

$$\sigma_{I}(g) = 0.968\sigma_{\chi}\lambda_{6-31G} - 0.009 \qquad (r_{c} = 0.992, f = 0.08)$$
(9b)

As can be seen in Figure 2, the plot of $\sigma_I(g)$ against $\Delta\iota\lambda$ is slightly more scattered than that against $\sigma_{\chi}\lambda$. The reason may be attributed to the incomplete evaluation

of $\sigma_1(g)$, because $\Delta_i \lambda$ correlates excellently with σ_i , as shown later. According to the results expressed by equations (8a) and (8b) and (9a) and (9b), it is obvious that the evaluation of λ on the basis of approximation at the 4-31G level is favourable with respect to the field parameter, $\Delta_i \lambda$, but that based on approximation at the 6-31G level is better for the field parameter $\sigma_x \lambda$.

The reasoning could be an accidental result due to the following data in the range of the limited substituents. The $\Delta \iota$ values correlated with the $(1 - q_H)$ values of H-X molecules calculated at the 4-31G level slightly better than those at the 6-31G level ($r_c = 0.950$ vs 0.946), and the σ_x values correlated with those at the 6-31G level slightly better than those at the 4-31G level ($r_c = 0.989$ vs 0.983), because the σ_x values were obtained based on the $(1 - q_H)$ values calculated at the 6-31G^{*} level.

Hence it seemed that the introduction of a new parameter, namely the charge separation parameter, λ ,¹⁹ is necessary in order to identify the reason for the non-linear relationship between the field effect and the substituent electronegativity parameter.^{3b,10,11}

The validity of the charge separation parameter (λ) becomes clear by comparing Figure 2 with Figure 5 in Ref. 10b [extremely scattered plot of σ_F (or σ_I) against σ_{χ}], because of a remarkable improvement in the non-linear relationship between σ_F (or σ_I) and electronegativity.

A linear relationship between $\Delta i \lambda$ or $\sigma_x \lambda$ and the field parameter, σ_i ,³⁴ was found with high precision as follows:

 $\sigma_i = 0.356 \Delta_i \lambda_{4-31G} - 0.013 \qquad (r_c = 0.991, f = 0.087)$

and

σ

$$r_i = 0.702\sigma_x \lambda_{6-31G} - 0.006$$
 ($r_c = 0.977, f = 0.14$)

Individual substituents used in the statistical analysis were H, CH₃, NH₂, OCH₃, OH, F, CF₃, COCH₃, CO₂CH₃, CN and NO₂. A similar treatment was also applied to other field parameters, F^{35} and $\sigma_{F(theor)}$,¹⁷ and the following linear relationships having a slightly less precise linearity were obtained; $F = 0.669\Delta \iota \lambda_{4.31G}$ + 0.073 ($r_c = 0.963$, f = 0.17, n = 12); $F = 1.355\sigma_x \lambda_{6.31G}$ + 0.073 ($r_c = 0.974$, f = 0.145, n = 12); $\sigma_{F(theor)} =$ $0.414\Delta \iota \lambda_{4.31G} + 0.007$ ($r_c = 0.930$, f = 0.22, n = 13); $\sigma_{F(theor)} = 0.861\sigma_x \lambda_{6.31G} + 0.006$ ($r_c = 0.961$, f = 0.16, n = 13).

In the plot of σ_i against $\sigma_\lambda \lambda_{6-31G}$, substituent groups such as CF₃, COCH₃ and OH deviated from the regression line. On the other hand, in the plot of *F* against $\Delta \iota \lambda_{4-31G}$, OCH₃, NH₂, CO₂H and NO₂ groups deviated considerably from the regression line. In the relationship between $\sigma_{F(\text{theor})}$ and $\Delta \iota \lambda_{4-31G}$, a larger deviation from the regression line was observed for CHO and NO₂ groups.

(10)

Energy decomposition analysis for isodesmic reaction

It is generally observed from the results in Tables 4 and 5 that the ΔE value consists mainly of an electrostatic (*ES*) term at longer distances ($r' = 4 \cdot 5$ Å or above), but the other energy terms such as *PL*, *CT*, *EX* and *MIX* contribute to the ΔE value to various extents at shorter distances ($r' = 2 \cdot 0 - 3 \cdot 5$ Å) in both series 2 and 3. In the case of 3 (X = F) (see Figure 3), the ΔE value changed from stabilization (negative value at r' = 3 Å or above) to destabilization (positive value at $r' = 2 \cdot 0 - 2 \cdot 5$ Å) with a decrease in the distance between two species (HF and HCO₂⁻). This result is ascribed to the sum of both stabilization due to an increase in *ES*, *CT* and *PL* terms and destabilization caused by an increase in *EX* and *MIX* terms.

The relative component energies (i.e. δPL , δCT , δEX and δMIX) in reactions (2) and (3) at a longer distance $(r' = 4 \cdot 5 \text{ Å})$ play only a minor role compared with the electrostatic energy term (δES), as shown in Tables 5 and 6. The point to be noted is that the electrostatic term (δES) is also dominant at a shorter distance $(r' = 2 \cdot 5 \text{ Å})$, although other terms such as δPL , δCT , δEX and δMIX show a considerably greater contribution than those at longer distances.

In general, the relationship between the relative electrostatic energy, δES (see Tables 5 and 6), and σ_F^{26} shows excellent linearity as follows: $r_c = 0.984$ at r' = 4.5 Å and $r_c = 0.978$ at r' = 2.5 Å for reaction (2), and $r_c = 0.982$ at r' = 4.5 Å and $r_c = 0.976$ at r' = 2.5 Å for reaction (3).

As shown in Figure 4, the δES value is nearly correlated with $\Delta i\lambda$ at a closer distance (at r' = 2.5 Å in 2 and 3). This trend was also generally observed in the isodesmic reactions at a longer distance (r' = 4.5 Å).

The magnitude of the energy $(\Delta E = 9.78 \text{ kcal mol}^{-1})$ in the charge-dipole interaction (in the case of $O_2N-H\cdots H-NH_3$ at r' = 4.5 Å listed in Table 3) is



Figure 4. Relationship between δES and $\Delta \iota \lambda$ in reactions (2) and (3) at r' = 2.5 Å

more than ten times of that of the relative energy $(\Delta E = 0.87 \text{ kcal mol}^{-1} \text{ at } r' = 4.5 \text{ Å}$, as shown in Table 3) in the case of the dipole-dipole interaction $(O_2N-H\cdots H-NH_2)$. Consequently, the field effect due to charge-dipole interaction becomes more important than that due to dipole-dipole interaction. As mentioned in the Introduction, the reason why the field effect for $\Delta p K_a$ is dominant in the charged molecules, $XCH_2CO_2^-$, but the electronegativity of the substituent correlates linearly with the chemical shift parameter $(\delta_{CH_2} - \delta_{CH_3})$ in the neutral molecules (XCH_2CH_3) may be attributed to the fact mentioned above.

Application of $\Delta_i \lambda$ or $\sigma_{\chi} \lambda$ to $\Delta p K_a$ and some physical data

The relative pK_a values (ΔpK_a) of a wide variety of aliphatic acids^{20,21,27,28} were analysed with high precision using $\Delta i \lambda$ or $\sigma_x \lambda$ as shown in Table 7.

$$\Delta p K_{\rm a} = \alpha \Delta \iota \lambda_{4-31\rm G} + c \qquad \text{or} \qquad \beta \sigma_{\chi} \lambda_{6-31\rm G} + c' \quad (11)$$

These results support the validity and generality of the λ parameter. The ionization energies of the lone pair on the nitrogen atom in 4-substituted quinuclidines (14)²² were also precisely related with $\Delta \iota \lambda$ or $\sigma_{\chi} \lambda$ (see Table 7).

From the analysis with equation (11) it was confirmed in the aliphatic systems that the electrostatic dipolar field effect on the reaction centre is much more important than the through- σ -bond effect.

Recently, Adcock and co-workers²³ reported that ¹³C-SCS of the C-4 atom for 4'-substituted bicyclo-[2.2.2]octylbenzenes (4) are proportional to σ_F , even though the atoms are contained in the unsaturated probe linkage. In this case, the C-4 SCS are also well correlated with $\Delta i \lambda$ or $\sigma_X \lambda$, as shown in Table 7.

Hence the validity of introduction of the charge separation parameter (λ) into the relationship between the field parameter and the electronegativity or inductive substituent parameter was best judged by comparing physical and chemical data such as $\Delta p K_{a}$, ^{20,21,27,28} *IP*, ^{20,22} ¹³C-SCS^{23,29} and log(k/k_0)^{20,30,31} with the parameter $\Delta \iota \lambda$ or $\delta_{\chi} \lambda$ as shown in Table 7.



The α (=0.58) [or β (=1.13)] value of the slope for 11 in Table 7 is considerably smaller than those for 9 (α = 0.75 or β = 1.49) and 10 (α = 0.79 or β = 1.65), although the geometrical relationships between the substituent and COOH group are nearly same. However, it is known that the substituent effect for 11 is almost same as those for 9 and 10, when the H atom and CH₃ group are omitted.³⁶ Therefore, the difference in slopes may be attributed to a deviation of H and CH₃ in 11.

It is concluded that both the charge separation parameter (λ) and substituent electronegativity are essential parameters for interpreting the electrostatic field effect. Our approach on the basis of the inductive substituent parameter (ι) and the charge separation parameter (λ) will be very useful as a means of predicting the field parameter (σ_F). Hence these results should cast a new light on an interpretation of the electronic substituent field effect in aliphatic series.

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